

Patent Application

for

**SYSTEM AND METHOD FOR
ESTIMATING CONDUIT LIQUIDITY REQUIREMENTS
IN ASSET BACKED COMMERCIAL PAPER**

by

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**SYSTEM AND METHOD FOR
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IN ASSET BACKED COMMERCIAL PAPER**

5 This application claims priority to U.S. Provisional Patent Application Serial No.
60/245,476, Filed November 3, 2000, entitled System and Method for Estimating
Conduit Liquidity Requirements in Asset Backed Commercial Paper, the disclosure of
which is incorporated herein by reference.

BACKGROUND

1. Field of the Invention

10 The present invention relates to a method and system for estimating the liquidity
requirements for pools of assets. In particular, the present invention relates to a method
15 and system for measuring the liquidity needs of pools of assets whose funding needs are
related to their issuers' ability to access the commercial paper markets.

2. Description of the Related Art

20 As known to those of ordinary skill in the art, commercial paper ("CP") is a short
term unsecured promissory note, typically issued by a corporation. Commercial paper
offers a low-cost alternative to a bank loan, allowing the issuer to quickly raise funds
without a complex or expensive Securities and Exchange Commission ("SEC")
registration. As such, corporations rely on exemptions under the Securities and Exchange
Act (such as under Section 3(a)(3) of the 1933 Act) to avoid the requirements for
registration of their commercial paper. This exemption requires that the paper be a short-
25 term security with certain characteristics. The maturity is limited to less than 270 days
and the notes are of a type that is ordinarily not purchased by the general public. In

practice this means that the notes have maturity of about 30 days, and minimum denominations are often between \$100,000 and \$1,000,000.

Because financing needs of the corporation often run beyond the typical 30 day maturity of commercial paper, the corporations need to roll-over the paper (i.e., issue new commercial paper on or before the maturity date), and have sufficient liquidity to satisfy the obligation if they are unable to roll-over the paper. The liquidity may be provided by bank lines-of-credit and cash reserves of the corporation.

Of course, as with any financial transaction, there are instances where the financial needs and credit-worthiness of a corporation changes (rating change) and the corporation is unable to roll-over the paper, or is required to pay the obligation from their cash reserves or draw on their line-of-credit. There are also instances where the corporations default on their commercial paper. As a result, there is historical data available to show probabilities of rating changes as well as the need for corporations to draw on their liquidity.

While corporations and other entities issue commercial paper as unsecured instruments, as described above, it is also known for entities to issue a form of commercial paper that is called asset-backed commercial paper. Asset backed commercial paper ("ABCP") ties the risk of the paper directly to the creditworthiness of specific financial assets, typically some form of receivable. These various known aspects of commercial paper and asset backed commercial paper are generally described in ABCP Market: Firmly established and still expanding, J.P. Morgan, May 23, 2000, (the disclosure of which is incorporated herein by reference).

At present, the liquidity needs of assets whose funding needs are related to their issuers' ability to access the commercial paper markets are met by financial guarantees and/or loan commitments sized at 100% of the related commercial paper program.

Although diversification benefits exist across pools of these assets, financial institutions

5 who provide these guarantees are unable to take advantage of these diversification benefits. As a result, in order to support the liquidity needs of a pool of these diverse assets, financial institutions must provide a very large amount of liquidity, i.e. 100% of the commercial paper programs of the supported assets. This is expensive and inefficient. Many financial institutions are reaching the limits of their ability to provide
10 this liquidity.

It is known to provide less than 100% liquidity for certain ABCP. These known circumstances are strongly related to the underlying assets and performance characteristics of the underlying assets. Eureka! is an example of one such proposal. However, reduced liquidity is not available for all ABCP, or at least a much broader
15 range of ABCP.

Methods and systems are needed to provide a means for assessing the true liquidity needs of pools of these assets. This allows for the more efficient use of the limited resource, i.e., the balance sheets of the financial institutions, resulting in lower costs, greater efficiency, and more supply of liquidity in the marketplace.

20 The preceding description and citation of the foregoing documents is not to be construed as an admission that any of the description or documents are prior art relative to the present invention.

SUMMARY OF THE INVENTION

In one aspect, the instant invention provides a method and system for managing liquidity requirements of asset backed commercial paper by determining a full liquidity
5 requirement for commercial paper commitments of at least one financial institution, and determining ratings of assets backing the commitments. Then, determining probabilities of rating changes of the assets, and calculating a liquidity requirement for the commitments that is less than the full liquidity requirement for the commitments using at least the ratings and probabilities of rating changes.

10 In another aspect, the instant invention provides a method and system for issuing asset backed commercial paper by receiving a liquidity commitment from at least one financial institution for a particular asset backed commercial paper issue. The liquidity commitment assures full liquidity for the particular commercial paper issue and represents less than full liquidity for a portfolio of asset backed commercial paper issues.
15 The less than full liquidity is determined by ratings of the assets backing the portfolio and probabilities of rating changes of the assets backing the portfolio. Then, issuing the particular asset backed commercial paper.

In another aspect, the instant invention provides a method and system for investing in asset backed commercial paper, which has a liquidity commitment from at
20 least one financial institution. The liquidity commitment assures full liquidity for the particular commercial paper issue and represents less than full liquidity for a portfolio of asset backed commercial paper issues. The less than full liquidity is determined by ratings of the assets backing the portfolio and probabilities of rating changes of the assets backing the portfolio. Then, redeeming the particular asset backed commercial paper.

In another aspect, the instant invention provides a method and system for providing liquidity commitments to asset backed commercial paper, where the liquidity commitment assures full liquidity for the particular commercial paper issue and represents less than full liquidity for a portfolio of asset backed commercial paper issues.

- 5 The less than full liquidity is determined by ratings of the assets backing the portfolio and probabilities of rating changes of the assets backing the portfolio.

In another aspect, the instant invention provides a method and system for managing liquidity requirements of asset backed commercial paper by determining a full liquidity requirement for individual commercial paper commitments backed by a plurality
10 of financial institutions, calculating a reduced liquidity requirement for the commitments, and allocating the reduced liquidity requirement among the institutions. Then, receiving shared liquidity assurances from the institutions for the individual commitments.

In another aspect, the instant invention provides a method and system for issuing asset backed commercial paper by receiving from a plurality of financial institutions, a
15 shared liquidity assurance for a particular asset backed commercial paper issue. The shared liquidity assurance represents an allocation of less than a full liquidity requirement among the institutions. Then, issuing the particular asset backed commercial paper.

In another aspect, the instant invention provides a method and system for investing in asset backed commercial paper which has a shared liquidity assurance from a
20 plurality of financial institutions. The shared liquidity assurance represents an allocation among the institutions of less than a full liquidity requirement. Then, redeeming the particular asset backed commercial paper.

In another aspect, the instant invention provides a method and system for providing liquidity assurance to asset backed commercial paper as a member of a plurality of financial institutions by providing a shared liquidity assurance for a particular asset backed commercial paper issue. The shared liquidity assurance represents an allocation among the plurality of institutions of less than a full liquidity requirement.

Thus, the instant invention advantageously provides assurance for full liquidity, without requiring full liquidity.

The foregoing specific aspects and advantages of the invention are illustrative of those which can be achieved by the present invention and are not intended to be exhaustive or limiting of the possible advantages that can be realized. Thus, the aspects and advantages of this invention will be apparent from the description herein or can be learned from practicing the invention, both as embodied herein or as modified in view of any variations which may be apparent to those skilled in the art. Accordingly the present invention resides in the novel parts, constructions, arrangements, combinations and improvements herein shown and described.

BRIEF DESCRIPTION OF THE DRAWINGS

The foregoing features and other aspects of the invention are explained in the following description taken in conjunction with the accompanying figures wherein:

FIG. 1 illustrates an embodiment of a system according to the instant invention;

FIG. 2 illustrates an embodiment of elements of a system according to the instant invention;

FIG. 3 illustrates a ratings transition matrix according to an embodiment of the instant invention;

FIG. 4 illustrates a model flowchart according to an embodiment of the instant invention;

FIG. 5 illustrates a distribution of asset returns with rating change thresholds according to an embodiment of the instant invention;

5 FIG. 6 illustrates an example of distribution of extent of draw on liquidity facilities according to an embodiment of the instant invention;

FIG. 7 illustrates an example of a method according to an embodiment of the instant invention;

FIG. 8 illustrates aspects of the instant invention in one embodiment;

10 FIG. 9 illustrates aspects of the instant invention in one embodiment;

FIG. 10 illustrates aspects of the instant invention in one embodiment;

FIG. 11 illustrates aspects of the instant invention in one embodiment;

FIG. 12 illustrates aspects of the instant invention in one embodiment;

FIG. 13 illustrates aspects of the instant invention in one embodiment;

15 FIG. 14 illustrates aspects of the instant invention in one embodiment;

FIG. 15 illustrates aspects of the instant invention in one embodiment;

FIG. 16 illustrates aspects of the instant invention in one embodiment;

FIG. 17 illustrates aspects of the instant invention in one embodiment; and

FIG. 18 illustrates an embodiment of an asset backed commercial paper program,

20 as it is known in the prior art.

It is understood that the drawings are for illustration only and are not limiting.

DETAILED DESCRIPTION OF THE DRAWINGS

Referring to FIG. 18, a typical asset backed commercial paper (ABCP) program is illustrated. As it is known, banks or financial institutions (1802) provide liquidity commitments in the form of conduit liquidity to issuers of asset backed commercial paper (1804). These liquidity commitments serve as a back-up in the event that the issuers are unable to roll over their ABCP at maturity or pay off the ABCP with proceeds from the assets. The assets backing the commercial paper (1806) are frequently pooled and include various types of receivables, such as credit card receivables (1808) and mortgages (1810). These pooled assets have individual obligors (1812), who make payments that eventually flow to the issuer. The assets have respective credit ratings, which are established or determined by public rating agencies, such as Moody's. The issuers themselves (1804) also have a respective credit rating. Investors (1814) purchase the ABCP from the issuer (1804) and expect to receive at maturity a return of their principle with interest. At maturity, it is common for the issuer to roll the ABCP over, issuing new ABCP. This presupposes that the issuer (1804) will be able to access the CP market at or prior to maturity of the ABCP. Access to the CP market is highly dependent on the issuer's rating, and is also dependent on the rating of their assets (1806). If the issuer rating, or the asset rating declines, the issuer may be unable to access the CP market, and will therefore be unable to roll over their ABCP at maturity. In this event, in order to meet the requirements of the maturing ABCP, the issuer will need to draw on the liquidity commitments provided by the bank or financial institution (1802).

In general, without the instant invention, liquidity providers (1802) provide a full liquidity commitment (100%) for the ABCP issued to the investors (1814). This full

liquidity is seldom needed or drawn against, but it has been provided because it was difficult to determine a reduced liquidity level that would reliably assure liquidity.

Where liquidity is needed or drawn, there are probabilities associated with a new draw against the liquidity commitment, a continued draw after a previous draw and an extent of liquidity draw. However, without the instant invention, these probabilities are not considered in establishing the required liquidity for ABCP. Similarly, there are probabilities associated with default of the banks or institutions providing the liquidity commitments. However, without the instant invention, these probabilities are also not considered in establishing the required liquidity for ABCP.

10 With this background, the present invention provides a system and model to perform simulations of events in order to determine the likely extent of liquidity funding needs, and thereby determine a reduced liquidity level with an assurance that the reduced level can reliably satisfy any liquidity needs. The reduced liquidity funding level determined by the instant invention is a percentage of and is less than the full (100%)
15 liquidity requirement of the issuers.

As thus stated, the funding needs of the underlying assets are related to their issuers' ability to access the commercial paper markets. In turn, the issuers' ability to access the commercial paper markets is strongly related to the public rating agencies' credit rating of the issuers. These ratings may vary over time, and are a publicly
20 recognized reflection of the creditworthiness of the issuers.

There are at least three basic embodiments of the instant invention, with variations of each embodiment. In one basic embodiment, all assets are considered to be of the same class, and are modeled as such. In another basic embodiment, the assets are

considered to be individually unique, and are modeled as such. Finally, in another basic embodiment, the banks or institutions providing the shared liquidity commitments are considered to have probabilities of default or failure, and are modeled as such.

When the results provided by the present invention are incorporated into the financial structure of a special purpose vehicle, financial institutions providing liquidity to the underlying assets are able to realize the diversification benefits of the pool. In this manner, the invention allows reliance on a group of financial institutions to provide liquidity facilities to the underlying assets.

A System According To The Instant Invention

Referring to FIG. 1, an embodiment of system 100 of the instant invention includes a plurality of banks or institutions 102, with associated liquidity commitments to issuers of ABCP. These banks or institutions 102 are electronically connected to provider of aggregate liquidity 104. Banks 102 and provider of aggregate liquidity 104 are electronically connected to individual ABCP programs 106. Although not illustrated, the individual ABCP programs include issuers of the commercial paper, the assets backing the ABCP, and the investors purchasing the ABCP.

The electronic connections and communication infrastructure 108 are any of a number of different types of wired and wireless connections and in one embodiment includes the Internet.

Each of banks or institutions 102, provider of aggregate liquidity 104 and individual ABCP programs 106 include computer systems 200, an example of which is illustrated in FIG. 2. Computer system 200 includes individual components such as: central processor 202; memory 204; input/output 206; fixed code storage 208; and

removable code storage 210. The individual components are interconnected by system bus 212

A Method According To The Instant Invention

Historical statistics regarding the likelihood of public rating agency rating

5 upgrades and downgrades over time have been assembled by many parties, and are known as rating transition matrices. FIG. 3 illustrates one such rating transition matrix. Assuming that an issuer's current public rating is A (302), there is a probability associated with transition of that A rating to any other rating, including remaining at an A rating. These historic ratings migrations profiles can be used to predict the likelihood of future
10 ratings upgrades and downgrades.

When the public rating agencies' credit rating of the issuer's credit rating is lowered (i.e. the issuer is downgraded), the issuer's ability to access the commercial paper markets is adversely effected. This makes it more likely that assets whose funding needs are related to the issuer's ability to access the commercial paper market will "draw" on
15 the liquidity facility provided by the financial institution.

According to one embodiment of the instant invention, the ratings transition matrix specifies the probability of an entity in any given rating category moving to any other rating category over the course of a given month. These statistics have been published by the various public ratings agencies and are generally available. The instant
20 invention is based on an assumption of monthly simulations, and therefore a ratings transition matrix developed on a monthly basis is required. Where the ratings transition matrix is known on an annual basis, it is possible to reduce the annual matrix to its 12th root (and therefore convert it to a monthly basis). This is accomplished by:

$$i := 0..7, j := 0..7, v_{j,i} := \text{eigenvec}(M, \text{eigenvals}(M)_i)_j, k3_{i,i} := (\text{eigenvals}(M)_i)^{\frac{1}{\text{numyears}}}$$

$$M_One := v \bullet k3 \bullet v^{-1}$$

5 where:

M is the annual ratings transition matrix;

M_One is the matrix reduced to a shorter time frame (one month);

numyears is the number of periods of reduction (here 12) when reducing the annual matrix to a monthly basis;

10 *eigenvec* represents the process of taking the eigenvectors of a matrix; and

eigenvals represents the process of taking the eigenvalues of a matrix.

Referring to FIG. 4, the method of the invention makes use of the strong relationship between funding needs (i.e., draws on liquidity facilities) and issuer ratings to predict future funding needs by predicting possible future ratings. Given the rating at each point in time, the probability of a new draw (402) is simulated, as well as the continuation of existing draws (404), and the extent (i.e., the amount or percent) of any given draw. The results of the simulation allow the generation of a distribution of probable draw amounts, and the specification of the likelihood of the draw amount. This allows the sizing of the required liquidity facility.

20 The method of the invention also determines the necessary characteristics of a group of financial institutions or banks which can provide liquidity facilities to the pool of underlying assets. In this aspect, the invention determines the confidence that the described group of financial institutions will be able to honor their obligations to provide

a given level of funding to the pool of underlying assets. This is based on the amount of liquidity provided by each institution or bank, the public rating agencies' rating of each institution or bank and the number of institutions or banks.

To determine the probability of a liquidity draw in each rating category, the system and method use a database of bank commitment experience to form the source for these calculations. The system and method then assemble dates of commitment origination, amounts of commitment and draw experience on a monthly basis. The system and method then estimate the liquidity draw probability statistics by observing the percentage of corporate commitments that have historically been drawn, arranged by rating category. Thus, the system and method simply take the average percentage in each rating category, observed with at least a monthly frequency. To develop confidence in the results, a long time frame is observed (e.g., seven or more years). Also, commitments which represent commercial paper backstop facilities are most appropriate for consideration.

Once the various probabilities of liquidity draw are determined, the system and method prepare the statistics by creating a histogram of the statistics. This histogram is arranged to specify the percentage of total observations of liquidity draws that fall in each percentile. For example, the histogram may specify what percentage of observed cases represent draws of 0-10% of the committed amount to that counter-party. Likewise, the system can specify how frequent 10-20%, 20-30%, etc. liquidity draws are in the historical database.

The system and method also access the historical commitment database to determine the probability of continued liquidity draw, once drawn. For each rating

category, the system and method observe all monthly datapoints during which a liquidity draw existed. Then, the system and method tabulate the percentage of the time that a liquidity draw was followed in the next monthly period by a continued liquidity draw. The system and method tabulate these percentages for each rating category.

5 In certain embodiments described in greater detail elsewhere, the system and method require estimates of asset correlation, where a correlation of 100% represents identical characteristics and a correlation of 0% represents no common characteristics. In one embodiment, these asset correlations are similar to stock price correlations. It is known that correlations of returns among the stocks in the S&P 500 have varied widely
10 over the last 20 years, from lows in the range of 20% to highs upwards of 50%. The system and method determine similar correlations for the assets backing the commercial paper.

In one embodiment, the correlation parameter represents the asset return correlation between the underlying securities representing asset backed commercial
15 paper. As these securities are themselves diversified pools of assets with stable characteristics, these asset correlations are likely to be relatively low. These correlations are not likely to be directly observable, so guidance is drawn from general observations of the market at large, or from the public rating agencies who perform analyses on assets of these sorts.

20 Referring again to FIG. 4, the invention considers each time period t from 1 to T , (where a time period is a month and the total time is typically 5 years, or 60 months). For each of these time periods, the instant invention models several parameters for each of N entities.

Ratings Transition Simulation (406): This aspect of the invention starts by determining the current rating of the entity. This process involves a Monte-Carlo simulation of asset returns, which are mapped to ratings transition thresholds through the use of the previously described historical ratings transition matrices. This provides the probabilities of transition from any rating category to any other rating category for a given period.

Continuation of Draw Simulation (404): This aspect of the invention determines whether the particular entity's liquidity facility was in the "drawn" state in the previous period. If so, the model simulates the extension or termination of that liquidity draw.

New Draw Simulation (402): If the liquidity facility was not drawn in the previous period, the invention simulates the possibility of a new liquidity draw.

Extent of Draw Simulation (408): If, in the particular period, there is a new liquidity draw, the invention determines the extent of that liquidity draw.

Summation and Compilation (410): Finally, the results for many simulated periods are assembled and the invention determines the total liquidity draw requirements. For each of T periods, the total liquidity draw is determined, and stored. The maximum liquidity draw over the T periods is determined and represents one sample liquidity estimate. Many thousands, even tens of thousands of such simulations are performed, giving a distribution of possible outcomes. Given a desired level of confidence, a minimum or reduced liquidity requirement for the pool of assets can be determined from the distribution of outcomes.

These general aspects of the invention are described in greater detail below.

In one embodiment, all assets are considered to be of the same class. However, there may be instances where it is desirable to treat the asset classes differently. Accordingly, the invention also includes approaches for dealing with various asset classes:

5 Modeling Diverse Assets:

In one embodiment, the system and method of the instant invention use a modified ratings transition simulation to allow for the modeling of diverse asset classes, using multiple transition matrices. This embodiment is appropriate for cases in which there exist various asset classes within the pool of assets. These asset classes may have
10 characteristics which necessitate the modeling of their ratings transitions separately.

There are at least two different techniques in this embodiment. One technique uses a "virtual asset portfolio" based on the "diversity score" of the actual assets. The other technique uses the explicit definition of the actual asset portfolio correlation and the actual asset portfolio, and does not therefore require the "diversity score" to generate a
15 "virtual asset portfolio".

The use of multiple transition matrices is useful when the asset classes have characteristics such that the simulation requires separate modeling of their rating transitions. Therefore, the asset class of each asset or pool of assets is provided among the inputs to the model, and these inputs are used to determine which of several transition
20 matrices are employed in the model.

A Virtual Asset Portfolio:

As one technique in modeling diverse assets, the virtual asset portfolio is based on the "diversity score" from the original asset portfolio. Using this virtual asset portfolio,

the required inputs to the system and method are only the ratings and maturity of the virtual assets, with uniform size assumed.

The virtual asset portfolio is assumed to have an asset return correlation of zero, and hence zero ratings transition correlation. It is derived by computing a "diversity score" from the original exact asset portfolio. This "diversity score" is the result of a calculation that is provided by the public ratings agencies, and is a measure of the concentration of a portfolio. The score represents the number of members of a diversification-equivalent "virtual" asset portfolio, whose assumed asset correlation is zero and whose constituents have equal weightings in the portfolio. This is a convenient vehicle to simplify the required simulation process in the model, while providing consistency with the rating agency risk analysis approach.

The invention creates the virtual asset portfolio with the same ratings distribution as the original portfolio, and with a maturity associated with each "virtual" transaction that represents the distribution of maturities of like-rated assets in the original portfolio. Each asset is assumed to have an equal size.

Once the virtual portfolio is created, the system and method only need to know the rating and maturity for each asset of the virtual asset portfolio as inputs to the model.

An Actual Asset Portfolio:

As one technique in modeling diverse assets, the explicit or actual definition of asset correlation is used. This technique is different from the "virtual asset portfolio", and does not rely on the "diversity score". Instead, the characteristics of the original asset portfolio are provided as an input to the model. In this technique, the asset returns are assumed to be correlated, and are modeled using a market factor to which each asset in

the portfolio is assumed to be correlated. This technique uses the following approach to generate the normally distributed asset return R .

$$R = \rho R_M + \sqrt{1 - \rho^2} \varepsilon,$$

5

where

- R_M is a standard normal variable representing the market factor,
- ρ is the square root of the average pair-wise asset correlations, and ε is a standard normal random variable.

10

Bank or Institution Failure: In one embodiment, the system and method consider characteristics required for a group of liquidity providers (e.g., banks and financial institutions), rather than a single provider, and probabilities that some members of the group of liquidity providers might fail or default.

15

This embodiment allows creation of a structure to employ the results of these models and also contemplates the formation of a group of financial institutions or banks to jointly provide liquidity to the underlying assets in the pool. The total size of the liquidity facility required is defined by the models described above. However, this requirement might not be simply split among a group of liquidity-providing financial institutions. Alternatively, the system and method take into account the possibility that one or more members of the group of financial institutions providing liquidity may be unable to meet their obligation to provide liquidity.

20

A model similar to the model above is employed to simulate defaults among the group of financial institutions or banks over the life of the transaction. For example,

assume R is the asset return over a given period, and is normally distributed. We construct a threshold Z_{Def} for R such that if $R < Z_{\text{Def}}$, the bank or financial institution is assumed to default. In this model, we use the cumulative probability of default over the life of the transaction (e.g., five years) as reported by historical rating studies published

5 by the ratings agencies. For example:

$$\text{Probability of default} = \text{Probability}(R < Z_{\text{Def}}) = \Phi(Z_{\text{Def}}/\sigma),$$

where, Φ represents the cumulative normal distribution.

For example, we can use this relationship to define the threshold points as follows,

10
$$Z_{\text{Def}} = \Phi^{-1}(\text{Probability of default}),$$

where, Φ^{-1} represents the inverse cumulative normal distribution.

R is generated as in the market factor model using the following construct:

15
$$R = \rho R_M + \sqrt{1 - \rho^2} \varepsilon,$$

where R_M is a standard normal variable representing the market factor, ρ is the square root of the average pair-wise asset correlations, and ε is a standard normal random variable.

By creating simulations of many thousands of transaction outcomes, we can

20 create a histogram of the number of defaulting financial institutions in the liquidity provider group, as well as a dollar distribution of liquidity available. This allows the estimate of these parameters at any given confidence level.

A Basic Embodiment:

The different embodiments and techniques described above will be discussed in greater detail with reference now to FIG. 3. An issuer's publicly assigned credit rating may migrate from the current rating to one of many different ratings over time. The model envisions the simulation of these movements on a periodic basis, repeatedly over the life of the transaction. These movements are simulated using a Monte-Carlo approach, in which a normally distributed random variable represents the entity's asset returns over each period. The invention assumes that there are asset values that correspond to different credit ratings at each point in time.

As illustrated in FIG 5, the normally distributed asset returns can be used to predict ratings transitions, by mapping different return levels to credit ratings transitions. By observing the likelihood of ratings transition from any rating category to any other rating category using the previously described historical ratings transition matrices, the invention maps the normally distributed asset returns to each possible ratings transition and defines thresholds for these transitions.

For example, assume R is the asset return over a given period, and is normally distributed. The invention constructs thresholds Z_{Def} , Z_{CCC} , Z_B , etc., for R such that if $R < Z_{Def}$, the entity is assumed to default. If $Z_B < R < Z_{BBB}$, then obligor is downgraded to BB, etc. For example:

$$\text{Probability of default} = \text{Probability}(R < Z_{Def}) = \Phi(Z_{Def}/\sigma),$$

where, Φ represents the cumulative normal distribution.

For example, the invention uses this relationship to define a threshold point as follows,

$$Z_{Def} = \Phi^{-1}(\text{Probability of default}),$$

where, Φ^{-1} represents the inverse cumulative normal distribution.

This approach is extended to define each of the asset return thresholds. Given the asset return thresholds, the normal random variable R , representing the asset returns for a given period, is used to determine the sample ratings transition for that entity for that

5 period.

In one embodiment, the generation of the normal random variable R is very simple, as asset correlation is assumed to be zero through the use of the "virtual asset portfolio" based on the diversity score of the original asset portfolio. See the description above for a discussion of the "virtual asset portfolio".

10 Continuation of Draw Simulation: The invention also determines whether the particular entity's liquidity facility was in the "drawn" state in the previous period. If so, the model simulates the extension or termination of that draw. This is performed by comparing a uniformly distributed random variable with the probability of a continuing draw for the current rating category. The probability of a draw continuing is defined by
15 historical analysis of like assets, with the same credit rating. Care must be taken to synchronize the historical data to the periodicity of the simulation (e.g., monthly historical data and monthly simulation path).

New Draw Simulation: Given that a particular entity's liquidity facility was not drawn at the beginning of a particular simulation period, the model simulates the
20 possibility of a new draw occurring during that period. This is performed by comparing a uniformly distributed random variable with the probability of a new draw for the current rating category. The probability of a new draw is defined by historical analysis of like assets, with the same credit rating.

Extent of Draw Simulation: If, in the particular period, there is a continuing or a new draw, the extent of that draw is then simulated. In this case, there exists a unique distribution of possible draw amounts, represented as a percentage of the total liquidity facility provided to that entity. This unique distribution is determined by an examination
5 of the historical draw history of like assets, of like credit rating. The distribution is described in an empirical manner, using an approach like that illustrated in FIG. 6.

The historical observations of extent of draw are assembled into deciles, from smallest to largest. A uniformly distributed random variable is then mapped to the deciles, allowing the simulation process to properly model the likelihood of various
10 "extent of draw" outcomes.

Assembly and Analysis of Results: For each of the T periods, the total liquidity draw for each asset of the N assets, during each simulation period is determined and totaled to arrive at a total liquidity draw for the period. This total amount for the simulation period is then stored. The total draws over each of the T periods are then
15 compared and the maximum liquidity draw is calculated. This maximum liquidity draw represents one sample liquidity draw estimate. Many thousands, even tens of thousands of such simulations are generated, giving a distribution of possible liquidity draw outcomes. This distribution is then analyzed and, given a desired level of confidence, a reduced liquidity requirement for the pool of assets is determined. To accomplish this, a
20 sorting algorithm is employed. Levels of confidence are then related directly to observations of the corresponding (percentile) position in the sorted list of samples. Linear interpolation is employed to derive levels of confidence that may lie between sorted samples.

Referring to FIG. 7, an embodiment of a method according to the instant invention is illustrated. At step 702, system 100 begins the method of the invention. At step 704, system 100 sets the number of Monte-Carlo simulation runs (SN), the number of time periods (T) and the number of assets or entities (N). In one embodiment, the number of Monte-Carlo simulation runs is 30,000, the number of time periods is 60 (months) and the number of assets or entities reflects the actual number of assets or pools of assets.

At step 706, system 100 sets a period counter (t) to 1, and at step 708, system 100 sets an entity counter (n) to 1.

At step 710, system 100 determines the rating of asset or entity n at time period t, and the associated probability of rating change during period t. As explained elsewhere in greater detail, the rating transition matrices may use a number of different possible embodiments and techniques.

At step 712, system 100 determines whether there was a liquidity draw for the asset during the previous simulation period. If so, then at step 714, system 100 determines the probability of the liquidity draw continuing, and if the liquidity draw continues, then at step 716 system 100 determines the extent of the continuing liquidity draw. In one embodiment the amount or percent of continuing liquidity draw is the same as the amount or percent of the previous liquidity draw. In another embodiment, the amount of the continuing liquidity draw is determined just as a new liquidity draw.

If there was no previous liquidity draw, then at step 718, system 100 determines the probability of a new liquidity draw, and at step 720, system 100 determines the extent of the new liquidity draw.

If there was any new or continued liquidity draw, then at step 722, system 100 adds the amount of the draw to the cumulative total for the respective simulation period.

At step 724, system 100 adds one (1) to n to increment the asset counter.

At step 726, system 100 determines whether n is greater than N , which would
5 mean that all assets have been considered during the simulation period. If n is less than or equal to N , meaning that more assets need to be considered for this particular simulation period, then system 100 loops to step 710, and continues the following steps so described.

If n is greater than N , meaning that all assets have been considered during this
10 simulation period, then at step 728, system 100 adds one (1) to t to increment the simulation period counter.

At step 730, system 100 determines whether t is greater than T , which would mean that an entire 60 month series of Monte-Carlo simulation periods have been completed. If t is not greater than T , then system 100 loops to step 708, and continues the
15 following steps so described.

If t is greater than T , meaning that an entire 60 month series of Monte-Carlo simulation periods have been completed, then at step 732, system 100 reviews the maximum liquidity draw for each simulation period, and stores the maximum liquidity draw for the Monte-Carlo simulation.

20 At step 734, system 100 subtracts one (1) from SN , to decrement the Monte-Carlo simulation counter.

At step 736, system 100 determines whether SN, the simulation counter, is equal to zero. If not, then system 100 loops to step 706, and continues the following steps so described.

If SN is equal to zero, then at step 738, system 100 ends the simulation by storing
 5 and then presenting an indication of the respective liquidity draw for each of the SN simulations.

An Example of the Instant Invention

In the following example, the invention determines the probabilities of liquidity draw and extent of the draw for a number of banks and their respective commitments.

10 In FIG. 8, at the beginning of the simulation model, one of the entities (Entity A) has 14 assets (802), each asset with a respective maturity (804) and rating (806) at the beginning of the model period. The simulation, or model will progress over 60 simulation periods, corresponding to 5 years. FIG. 8 is the state at the beginning of the first simulation period (808).

15 For each of the assets that has a rating, there is a respective ratings transition matrix. For example, asset 1 (810) has a rating of AA at the beginning (806) of simulation period 1. Referring to FIG. 10, we find the respective ratings transition matrix for an asset that has a rating of AA. As FIG. 10 illustrates, there is a high probability that the asset will remain rated AA, as compared to changing to a rating of A or AAA, or any
 20 other rating. Using a Monte-Carlo technique, and the ratings transition matrix, the model determines what the rating for that asset will be at the end (812) of the simulation period. For most assets the rating does not change. However, for some assets, the rating will improve, or decline. Thus, asset 5 (814), which begins the simulation period with a

rating of BBB+, ends the simulation period with a rating of A- (an improvement).

Alternatively, asset 7 (816), which begins the simulation period with a rating of A-, ends the simulation period with a rating of BBB+ (a decline).

The respective ratings transition matrix for asset 5 is illustrated at FIG. 11, while
5 the matrix for asset 7 is illustrated at FIG. 12.

After the model determines any ratings transition during the simulation period, the model determines whether there was a liquidity draw during the previous period (818). If there was a liquidity draw in the previous period, the model determines the probability of a continuing liquidity draw over the current simulation period. For this, the model uses a
10 similar probability distribution, such as illustrated in FIG. 13. For example as illustrated, if there was a liquidity draw in the previous simulation period, there is a probability that the liquidity draw will continue in the next simulation period, and also a probability that the liquidity draw will not continue. Using the same Monte-Carlo technique described above, the model determines whether the liquidity draw continues (819). Thus, in FIG. 8,
15 assets 8 (820) and 13 (822) both had previous liquidity draws before the beginning of simulation period 1. However, the Monte-Carlo simulation determines that only asset 13 has a continuing liquidity draw at the end of simulation period 1.

If the draw continues, the model then determines the extent of the liquidity draw. In one embodiment the extent of a continuing liquidity draw is the same as the previous
20 liquidity draw. Alternatively, in another embodiment, as illustrated in FIG. 17, the Monte Carlo technique determines the extent of the liquidity draw, in a similar manner as described above.

If there was no liquidity draw in the previous simulation period, then using the Monte-Carlo technique, the model determines whether there is a new liquidity draw over the current simulation period. This is accomplished in a similar manner, such as illustrated in FIG. 14. Here, we see that there is a small probability that a new liquidity
5 draw will occur, and a much larger probability that no new liquidity draw will occur.

If there is a new liquidity draw, the model then determines the extent of the liquidity draw. In FIG. 15, the Monte-Carlo technique determines the extent of the liquidity draw, in a similar manner as described above.

The amounts of any continued liquidity draw and new liquidity draw for the
10 particular asset, are calculated for the period (824), and the amounts for that period are totaled across all assets of the entity (826).

This Monte-Carlo process is repeated for each asset of each entity over the simulation period. After calculating liquidity draw and liquidity draw amounts, information such as illustrated in FIG. 8 is saved. Using this information at the end of the
15 first simulation period, the model starts the second simulation period. FIG. 9 illustrates a second simulation period (902). The same assets (904) are illustrated in FIGs. 1 and 2, and the respective times to maturity (906) for the simulation period have been updated (since each asset is one month closer to maturity).

The beginning rating for each asset (908) is the same as the ending rating (812)
20 from the previous simulation period. Using the same Monte-Carlo technique with the ratings transition matrix, an ending rating (910) is determined. A previous liquidity draw (912) is determined from the previous simulation period, and depends on whether there was a continuing liquidity draw or a new liquidity draw in the previous period. If there

was no continuing liquidity draw or new liquidity draw in the previous simulation period, there is no previous liquidity draw in the current simulation period.

Asset 8 (918), which had a liquidity draw prior to simulation period 1, did not have a continuing liquidity draw during period 1 and therefore there is no previous liquidity draw (912) for asset 8 at the beginning of simulation period 2. However, we saw in FIG. 8 that asset 13 had a continuing liquidity draw (819) during simulation period 1, and therefore in FIG. 9, asset 13 (920) has a previous liquidity draw (912) at the beginning of period 2. We also see that asset 13 had a continuing liquidity draw (914) in simulation period 2, and the liquidity draw amount for simulation period 2 (916) is added to the total liquidity draw (924) for simulation period 2.

We further note that asset 7 (922) has a new liquidity draw in simulation period 2.

The steps just described are repeated for all of the assets of all of the entities for all of the simulation periods (60). When maturity of an asset is reached the asset is removed from the simulation.

The liquidity draw amounts for each of the assets of each of the entities in each simulation period are totaled and the liquidity draws of all of the entities are totaled and stored. Using these stored totals, the invention determines a maximum liquidity draw for the simulation. This constitutes one full Monte-Carlo simulation. However, this does not provide sufficient probability data, and therefore this is repeated many times, typically on the order of 30,000 times. The maximum liquidity draw for each of those 30,000 or so simulations is saved and a histogram of the simulation results is prepared, such as illustrated in FIG. 16A. Here, the height of each bar represents the number of times the simulation yielded a maximum liquidity draw within the boundaries of the bin. The

probability distribution of FIG. 16A is converted to a cumulative probability distribution, such as illustrated in FIG. 16B. Using these histograms, and a desired assurance level, it is possible to determine the probabilities of different liquidity requirements. For example, if a 90 percent confidence is desired, the required minimum liquidity might be

5 15% of total commitments, while 95 percent confidence might require at least 20% liquidity of total commitments. Finally, 99 percent confidence might require at least 25% liquidity of total commitments.

The example description above has not considered the probability that any of the banks providing liquidity commitments would default, or be unable to meet their shared

10 liquidity requirements. Accordingly, in a similar manner, the system and method of the instant invention also performs a Monte-Carlo simulation of bank or institution failure or default for each of the simulation periods. Using this simulation, the invention determines the probability of failure or default and can determine and assess the required number of banks or institutions.

15 Although illustrative embodiments have been described herein in detail, it should be noted and will be appreciated by those skilled in the art that numerous variations may be made within the scope of this invention without departing from the principle of this invention and without sacrificing its chief advantages.

Unless otherwise specifically stated, the terms and expressions have been used

20 herein as terms of description and not terms of limitation. There is no intention to use the terms or expressions to exclude any equivalents of features shown and described or portions thereof and this invention should be defined in accordance with the claims that follow.

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